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Laboratoire Génie Industriel

Automating Collision Avoidance Maneuvers

On the use of available space monitoring data for improving the risk of collision avoidance

Prof. Adam F. Abdin, Assistant Professor

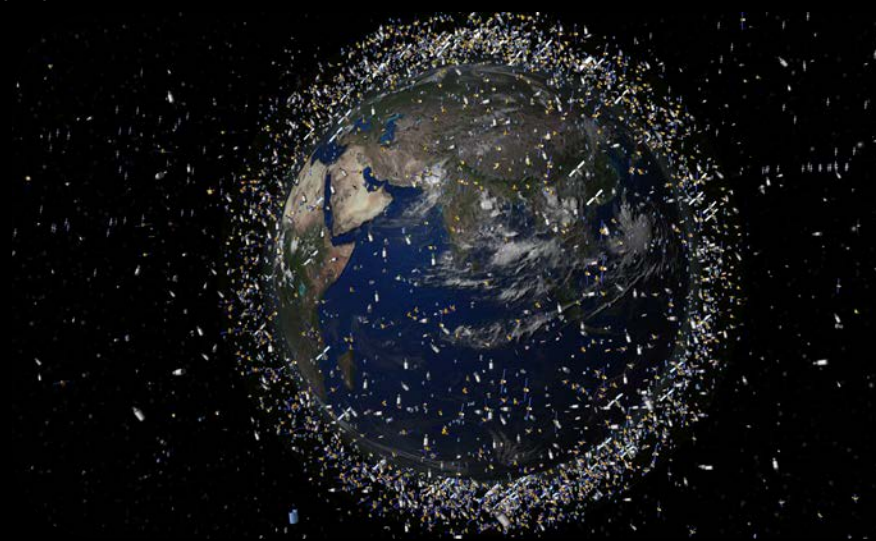
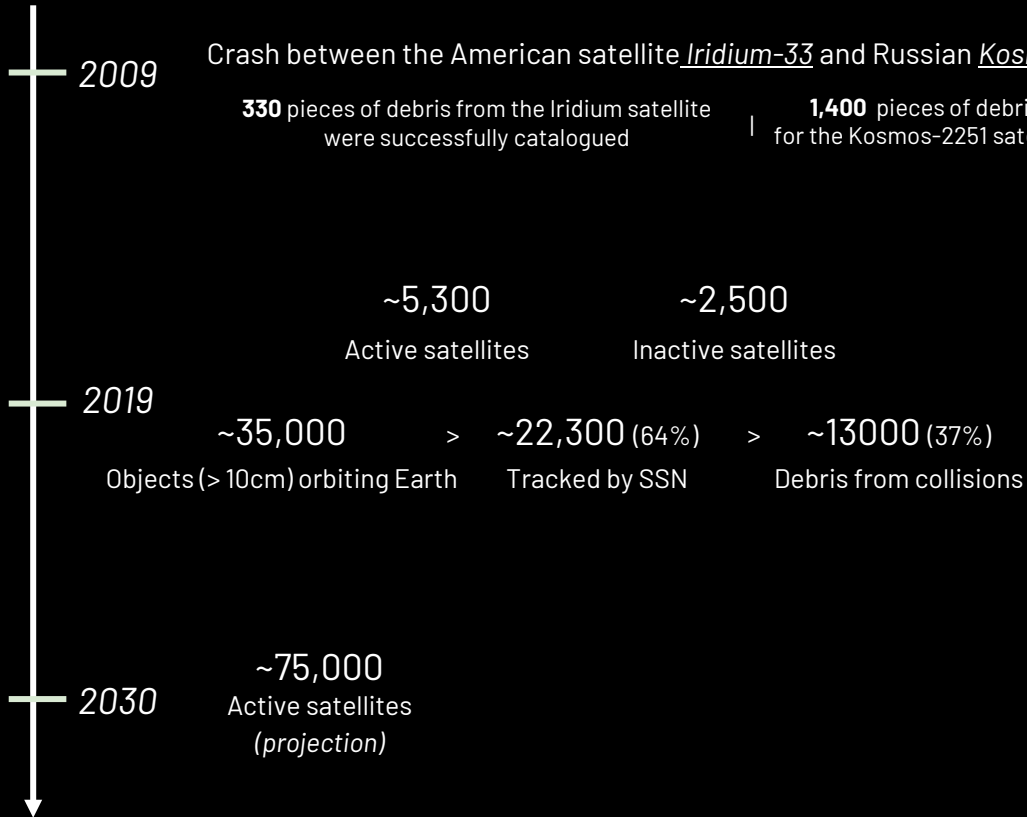
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Students : Nicolas BOURRIEZ; Adrien LOIZEAU; Susmitha Patnala



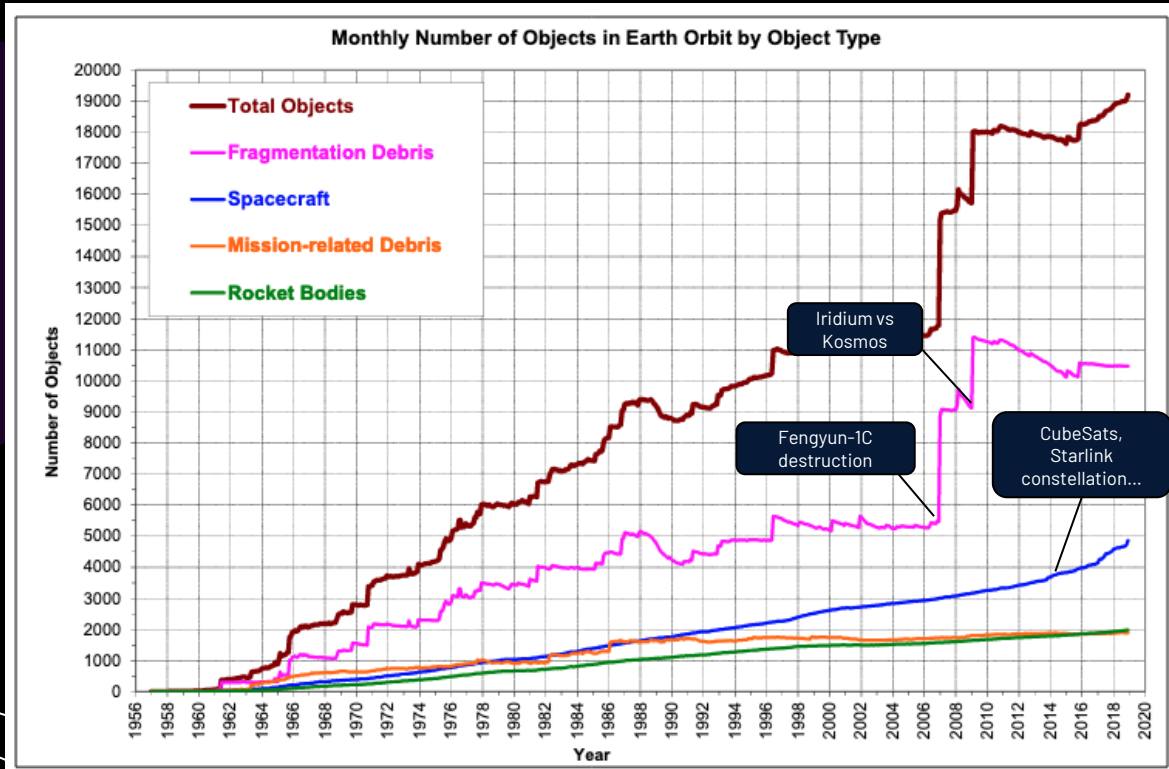
Kessler Syndrome



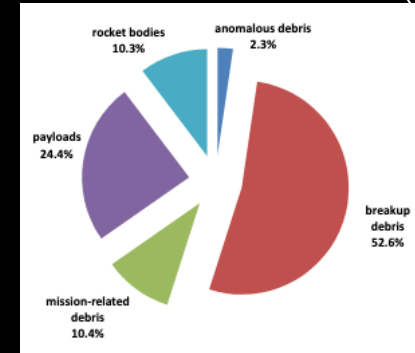
"Trending analysis of historical conjunction data messages", 2019

"Space Navigator: a tool for the optimization of collision avoidance maneuvers", 2019

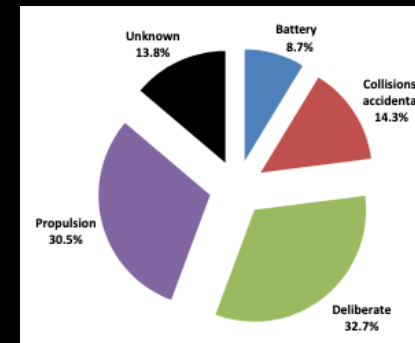
Orbit Debris Analysis



Summary of all objects in Earth orbit officially cataloged by the U.S. Space Surveillance Network since 1956



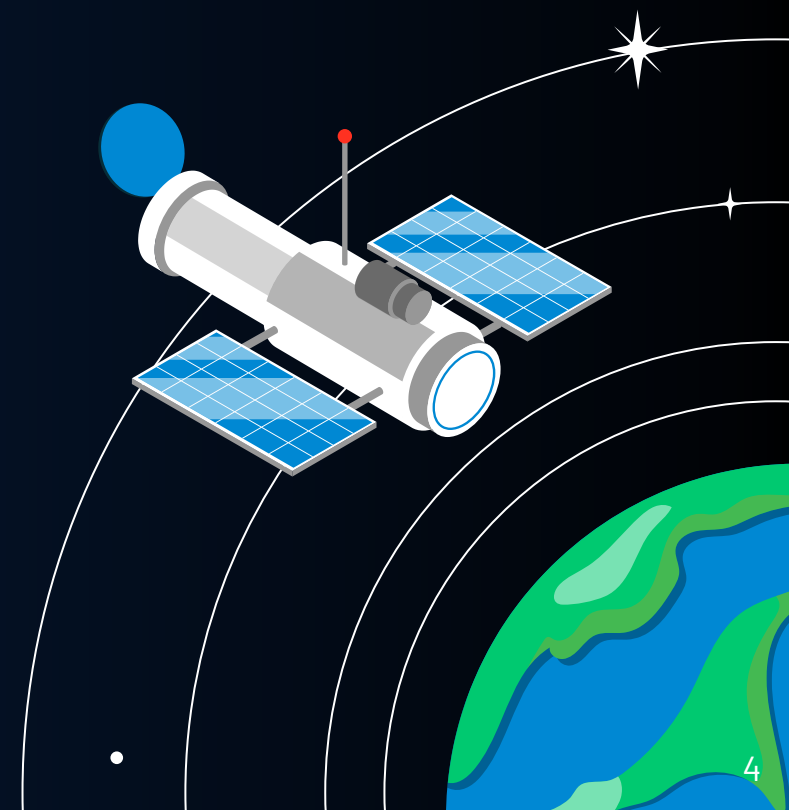
Types of debris



Causes analysed for spatial debris to be created in LEO



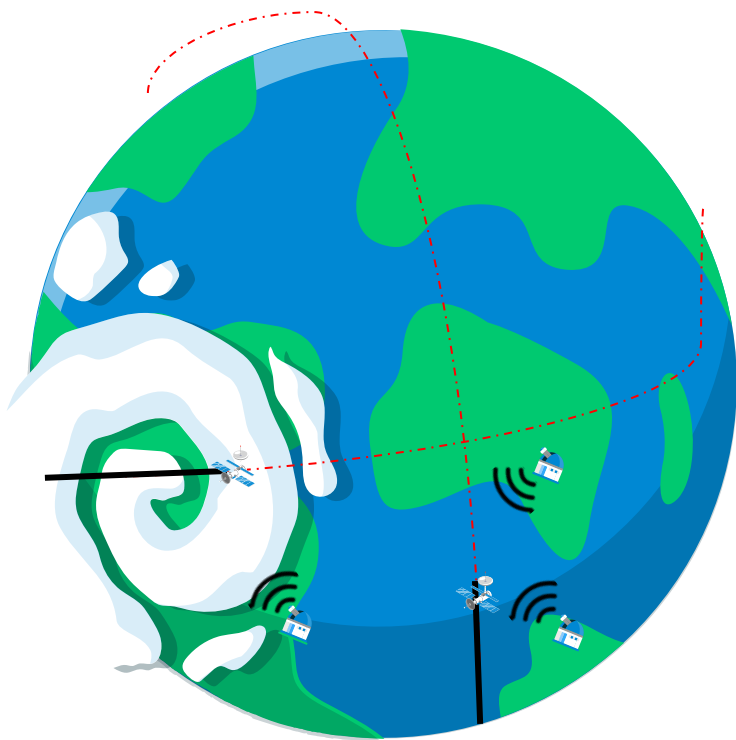
Data usage for Conjunction Assessment



Conjunction Event Prediction

- 22040 Catalogued items in space and many more uncatalogued
- Collision models –MASTER(ESA), ORDEM(NASA)
- Lethality of debris depends on size, but no consensus reached
 - Aluminum sphere of 1cm of radius at 14km/s = 1MJ = 1500kg car at 130km/h.
 - Aluminum sphere of 1mm of radius at 14km/s = 1KJ = bowling pin at 100 Km/h.¹
- Mean time between two successive collisions is inversely proportional to the size
- How to protect our spacecraft?? CAM → for debris > 10cm else severe damage(CAM)

Conjunction Event Prediction



Global Objective: Determine within 7 days into the future which space objects/**debris** will come within proximity/**cunjunction** of a primary/protected asset (i.e. a satellite)

Objects type: Near-earth orbiting objects (< 225min revolution)

How: Assess the future predicted positions of both objects

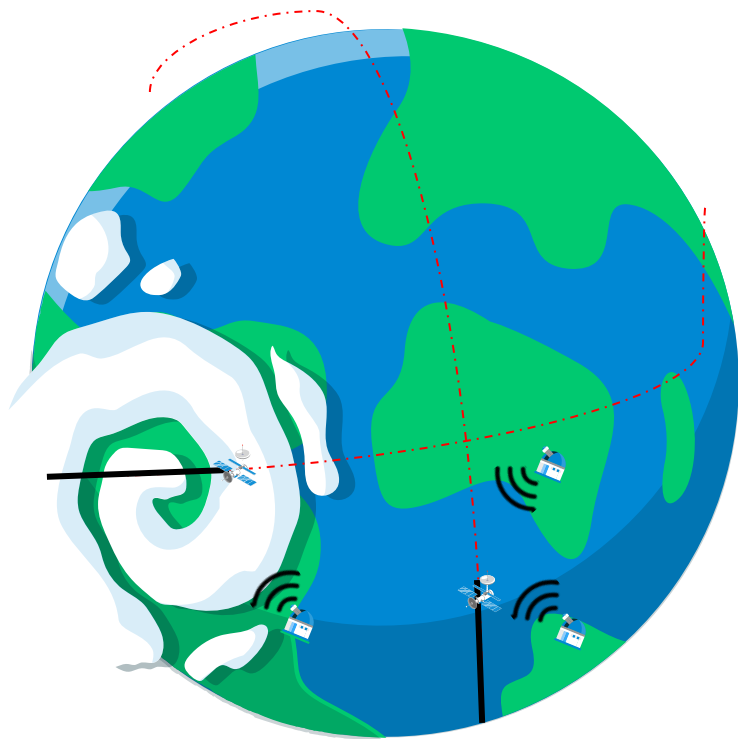


Raw TLE (Two-Line Elements) received from Sensors & Radars Tracking (TDRSS, C-band, GPS)



State vector & Covariance 7-day projection (/min)
(Simplified General Perturbations-4 propagator)

Conjunction Event Prediction



What is the uncertainty in the propagated orbits ?

- Normally distributed uncertainty [1]
- SGP4 model has an error ~ 1 km at epoch and grows at $\sim 1-3$ km per day [2]

What is behind the SGP4 Propagator algorithm ? [3]

1. **Long-term propagation** from **Keplerian elements**
(Line 2 of TLE)
1. **Short-term perturbations** from **external data**
(Line 1 of TLE)

[1] https://stacks.stanford.edu/file/druid:dg552pb6632/Foster-estes-parametric_analysis_of_orbital_debris_collision_probability

[2] <https://celestrak.org/publications/AIAA/2006-6753/AIAA-2006-6753.pdf>

[3] <https://celestrak.org/NORAD/documentation/spacetrk.pdf>

Conjunction Event Prediction

- European space surveillance network - EUSST database and catalogue → 7 EU states collab. [Source](#)
- US Space surveillance network - Open source data → TLE data - [Source](#)
- CDM US Joint Space Operations Center JSpOC
- SSN network

Conjunction Event Prediction

Initial Orbit Determination

- Principle (Kepler's method \rightarrow Taylor's expansion and dynamical model)
- Gauss method (3 pairs of angles) \rightarrow time-sequential and co-planar
- Gibbs method (3 position vectors) \rightarrow orbit from 3 position vectors

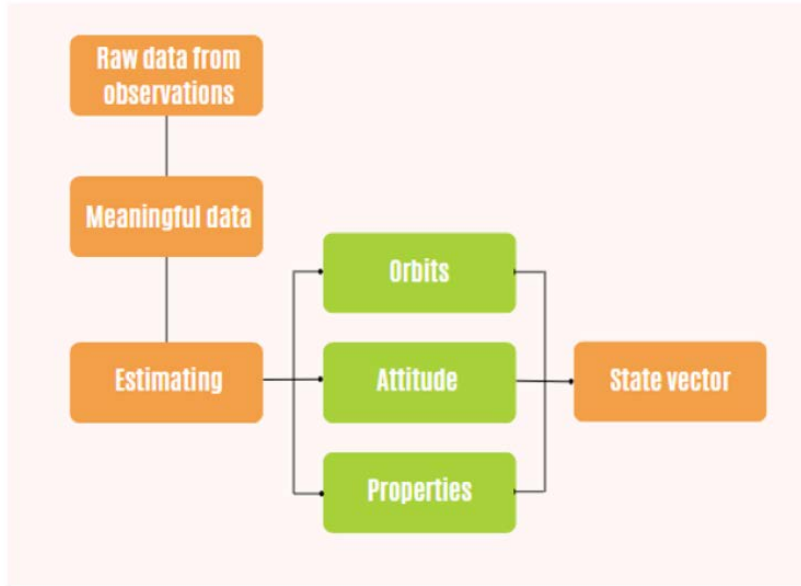
Orbit Determination

- Bayesian filtering \rightarrow prediction and correction
- Kalman filter (KF)
- Extended Kalman filter (EKF) \rightarrow For non-linear, we linearize using Taylor's expansion

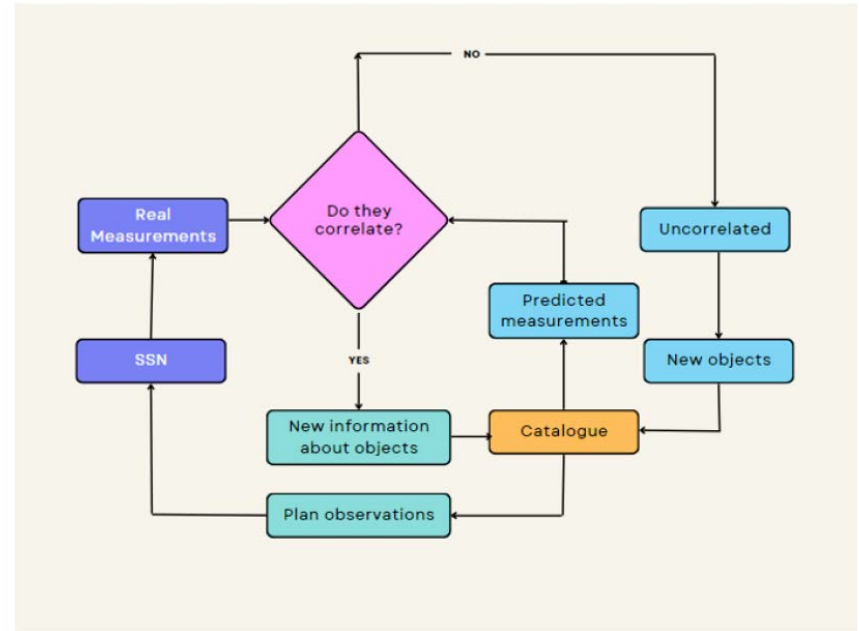
Collision Risk Assessment

- Close approach detection
- Collision Data Message (CDM)
- Probability of collision

Conjunction Event Prediction - Cataloguing by Space Surveillance Network (SSN)

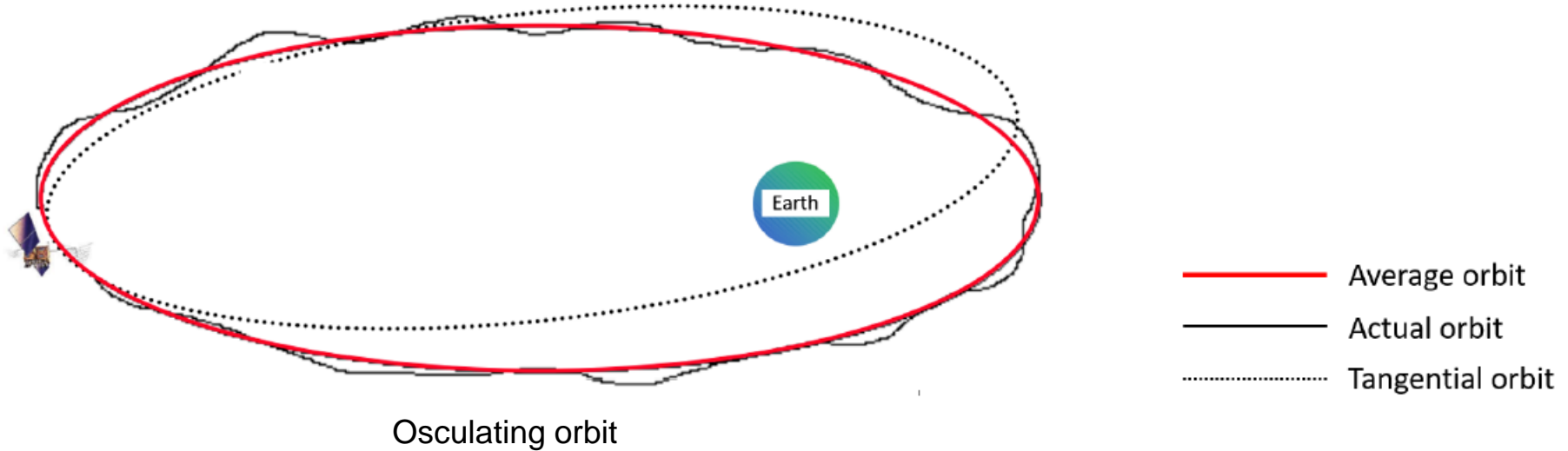


Initial Cataloguing



Catalogue update

Conjunction Event Prediction - Uncertainties Everywhere

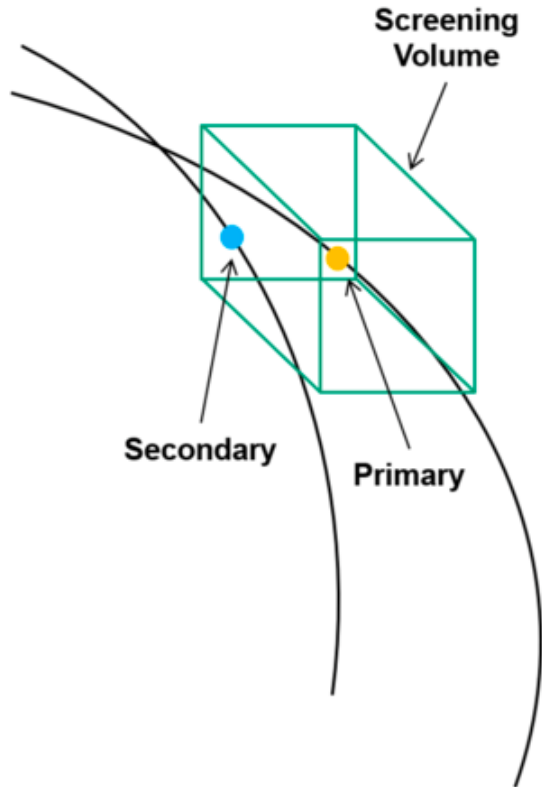


$a, e, i, \Omega, \omega, M \rightarrow$ Osculating parameters

Conjunction Event Prediction - Uncertainties Everywhere

- Size of orbital population is unknown, and time-varying
- Dynamics of orbital objects
 - Forces: Drag, Solar radiation pressure, Third-body, Earth potential...
 - External effects: Solar activity, Atmospheric density...
 - Behaviors: Unexpected manoeuvres of unknown nature
- Observation process of sensors
 - Measurement bias/noise, Atmospheric corrections
 - Missed detections, False positives
 - Origin object of measurement usually unknown

Close Approach Risk Assessment



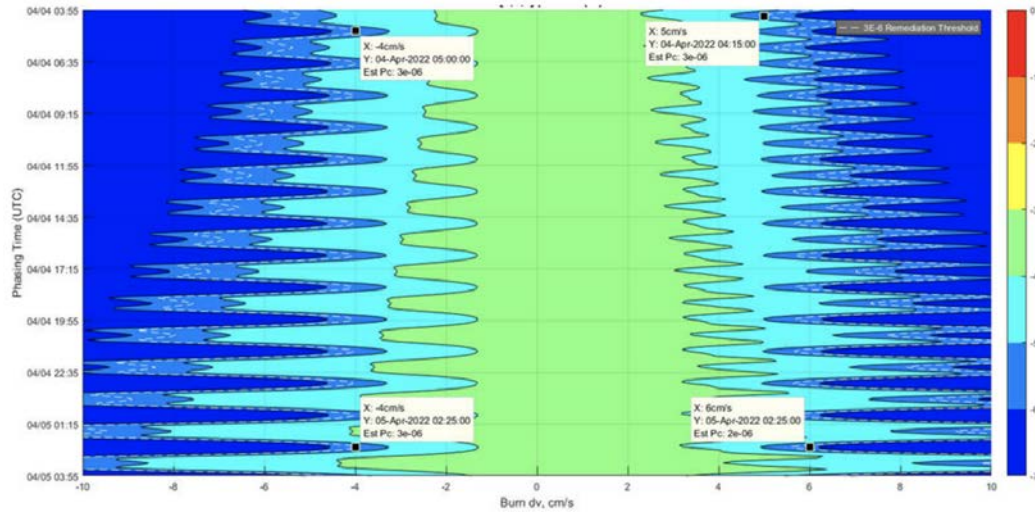
- Using projected trajectories, assess if secondary object enters **screening volume**
- Screening volume is centered on the primary object (i.e. satellite)
- **Probability of collision (Pc)**: likelihood that the actual miss distance between the two satellites will be smaller than their combined size

=> this likelihood calculation assumes a probabilistic form because the ephemerides used to identify the conjunction represent predictions with uncertainty

$$PoC = \frac{1}{2\pi |Det(C)|^{1/2}} \iint_{x^2+y^2 \leq d^2} \exp\left(-\frac{1}{2}(\mathbf{r} - \mathbf{r}_{S/P})^T C^{-1}(\mathbf{r} - \mathbf{r}_{S/P})\right) dx dy$$

- $\pi = 3.141592653589793$.
- C is the 2X2 projection of the combined 3X3 covariance at TCA onto the collision plane²².
- $Det(C)$ is the determinant of C .
- d is the sum of the two object sizes²³.
- “exp” is the exponential function, i.e., e to the power in parentheses with e = 2.718281828459045.
- $\mathbf{r} = (x, y)^T$ is any point in the collision plane such that $x^2 + y^2 \leq d^2$.
- $\mathbf{r}_{S/P} = (r_{S/P}, 0)^T$ is the position of the secondary relative to the primary along the x-axis in the collision plane.
- C^{-1} is the inverse of C .

Close Approach Risk Mitigation



Maneuver trade-space plot

- CDM sent 3 days prior
- Either *propulsion* system or *differential drag*
- Manoeuvre required when $PoC > 1E-04$ [4]

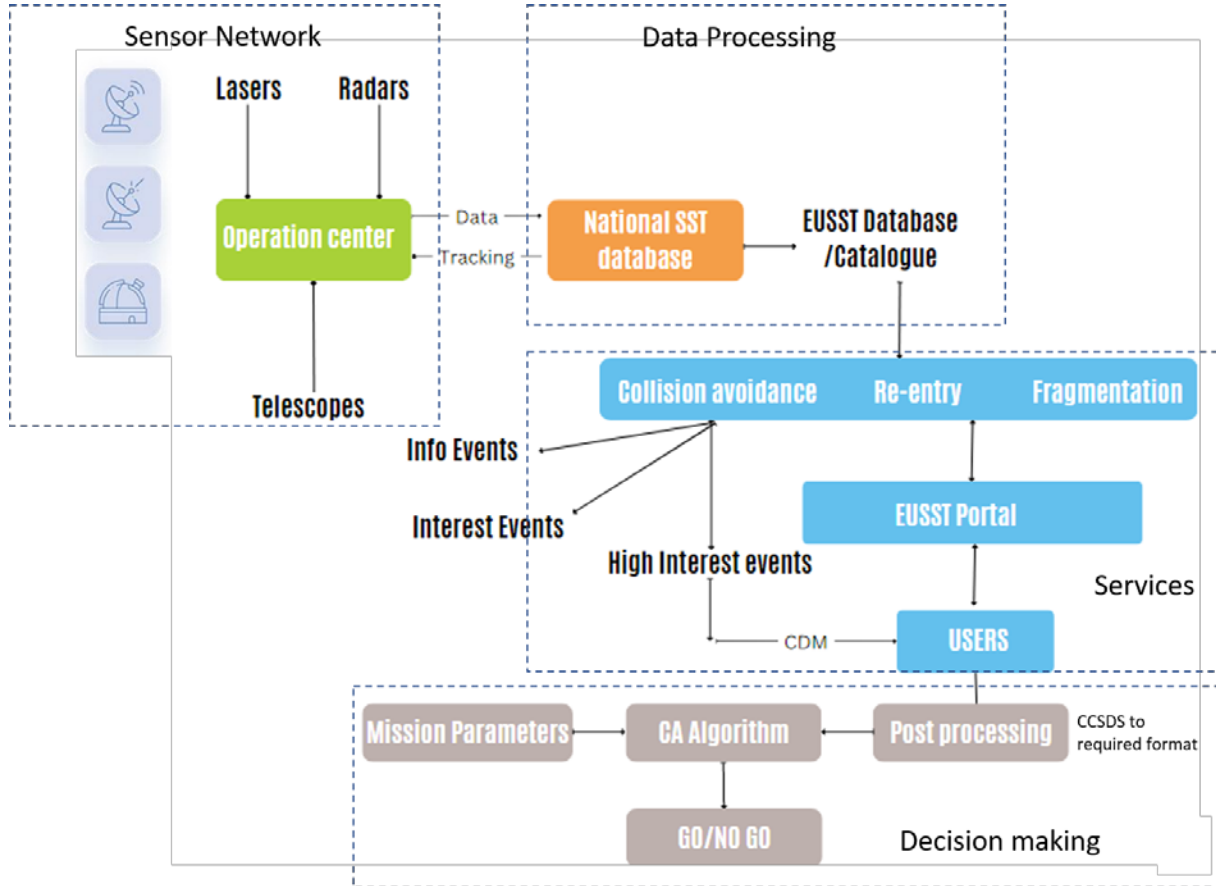
Existing data types

Data usage

TLE	CDM
Limited accuracy and precision Limited information Lack of real-time updates Assumes perfectly spherical earth	Provide precise and accurate information Detailed analysis of potential collision Timely updates Perturbations are included

Table: Comparison between TLE and CDM

From sensory data to decision making



Data handling framework

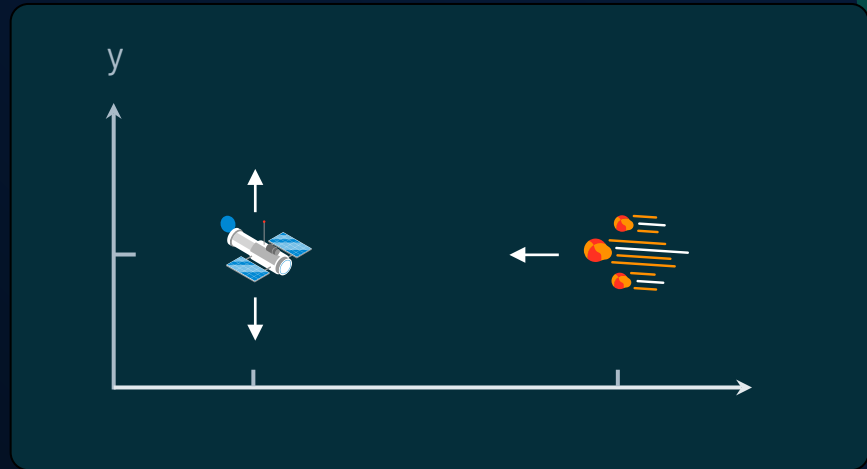
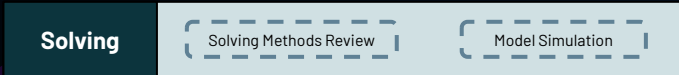
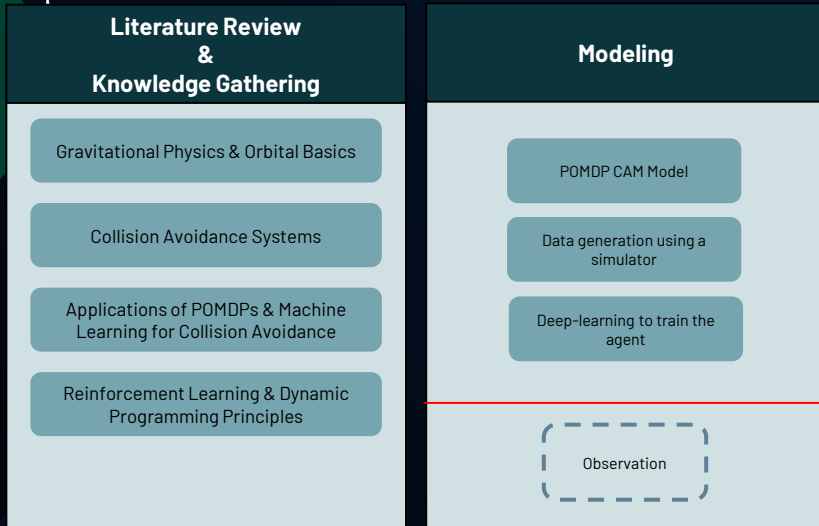
The background is a dark blue space-themed illustration. It features several white stars of varying sizes and shapes, some with four-pointed starburst patterns. There are also abstract, colorful shapes in shades of purple, blue, and green, resembling nebulae or galaxies. Two sets of white concentric circles are positioned on the left and right sides, representing orbital paths or sensor ranges. In the top right corner, there is a small logo consisting of a grey 'C' shape and a red 'S' shape. In the bottom right corner, there is a small white dot and the number '17'.

Automating Spacecraft Collision Avoidance



General Framework

Project Framework



POMDP:

$$\langle \mathcal{S}_{\text{states}}, \mathcal{A}_{\text{actions}}, \mathcal{O}_{\text{observations}}, \mathcal{T}_{\text{transition}}, \mathcal{R}_{\text{reward}}, \gamma \rangle$$

julia



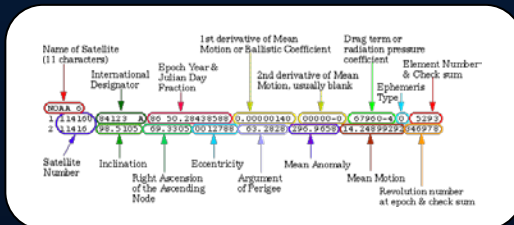
Collision avoidance



1. Data gathering



2. Data Format



3. Orbital projection (SGP4 perturbator)

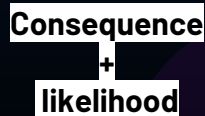


Cara: Conjunction Assessment Risk Analysis

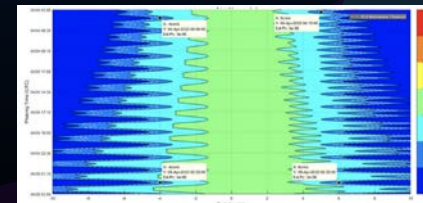
1. Conjunction Event Prediction



2. Close Approach Risk Assessment



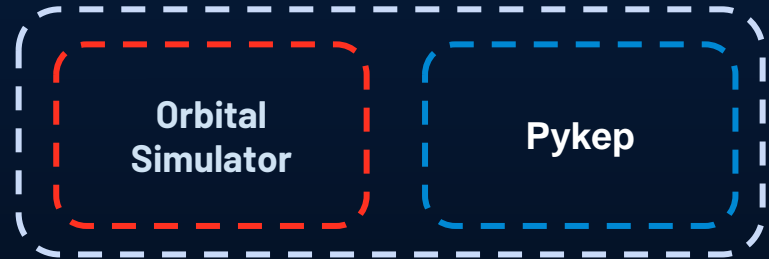
3. Close Approach Risk Mitigation



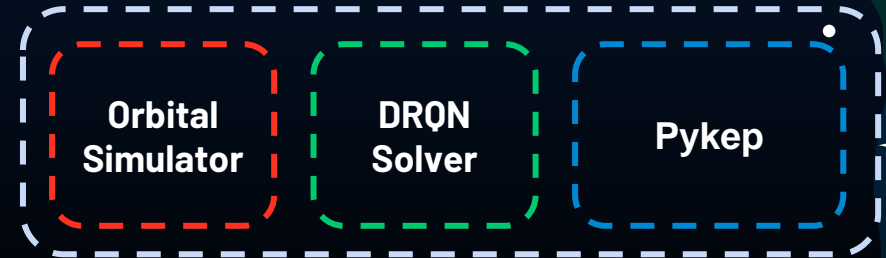
DATA FORMAT

- ✗ TLE
- ✗ Private databases
- ✗ CDM

Scarcity of collision data



Our proposed approach



Model: POMDP

$\langle \mathcal{S}, \mathcal{A}, \mathcal{O}, \mathcal{T}, \mathcal{R}, \gamma \rangle$

\mathcal{S} : Continuous

$u, v : (x, y, z, dx, dy, dz)$

\mathcal{A} : Discrete (625 actions)

[0.0, 0.01, 0.05, 0.1, -0.05, time]

\mathcal{T} : Model Free

\mathcal{O} : Epistemic noise from SGP4

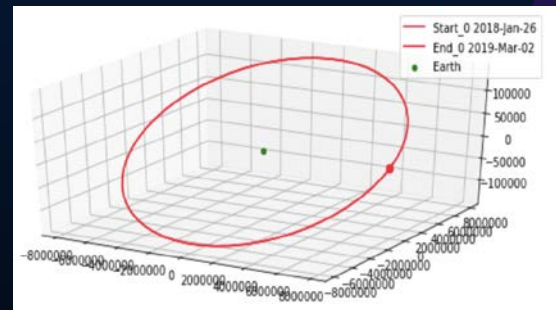
Noises from sensors

\mathcal{R} : Collision probability

Fuel level

Trajectory deviation

γ : Discounting rate



Solver - Deep learning

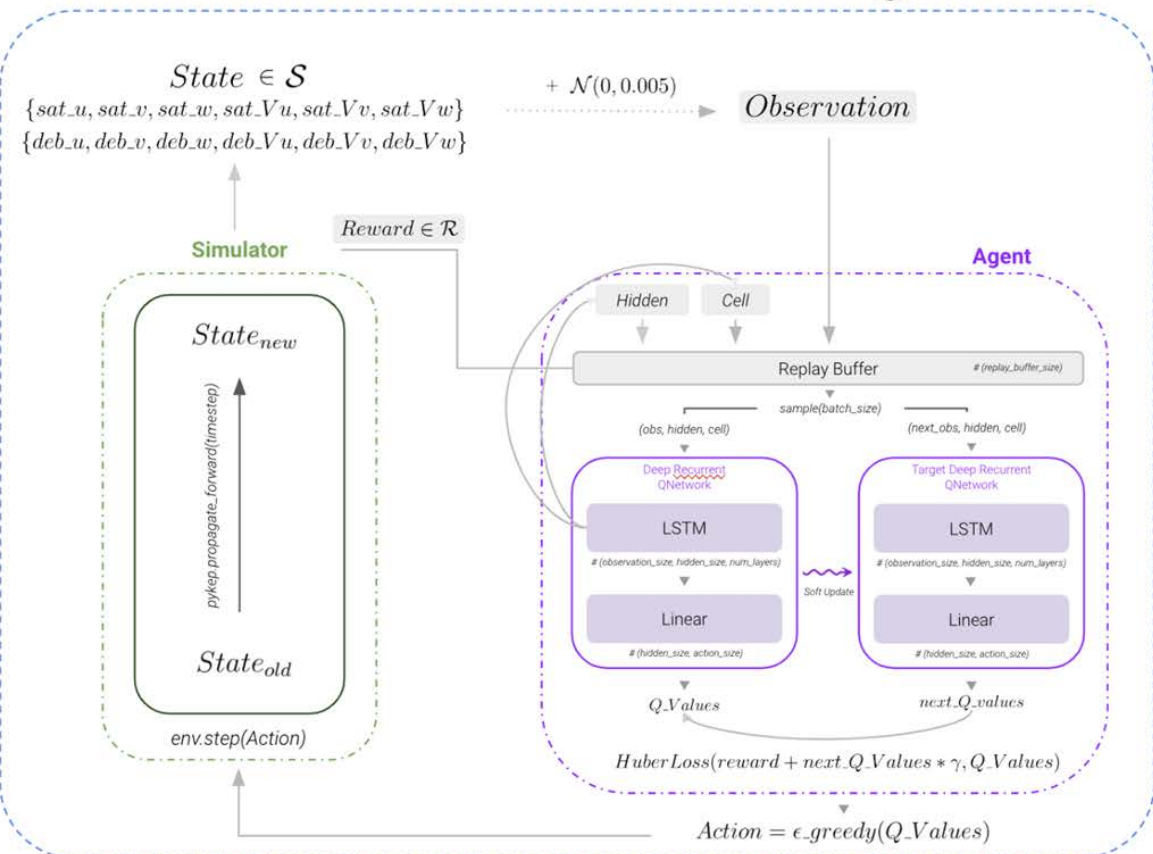


num_envs

num_steps_per_env

Environment Generator

- start_time $\sim \mathcal{U}(6600, 6700)$
- end_time $start_time + \sim \mathcal{U}(0.1, 10.0)$
- pos_sig $\sim \mathcal{U}(0.0, 0.1)$
- vel_sig $\sim \mathcal{U}(0.0, 0.1)$
- i_thresh $\sim \mathcal{U}(0.0, 1.0)$



SIMULATOR

- Simple pipeline:

TLE Data Collection (SpaceTrack **API**/ Celestrack
JSON)

Data Preprocessing (**tle-tools/pandas**)



Orbit Simulation (**poliastro**)



Next steps:

- *A more ready-to-use python simulator available ?*

DATASET

- Historical TLE dataset publicly available
- BUT no precision on conjunction events -> hard to train RL algo without conjunction situations

Next steps:

- *Generate artificial TLE ?*
- *Correlate CDM with TLE ?*

MODEL

- Actual simple pipeline helps understand the astrophysics -> helps to model the observations of our 3D problem
- BUT frequency of TLE data appears stochastic and object-dependent

Next steps:

- *Propagate each received TLE with SGP4 to a state vector ?*

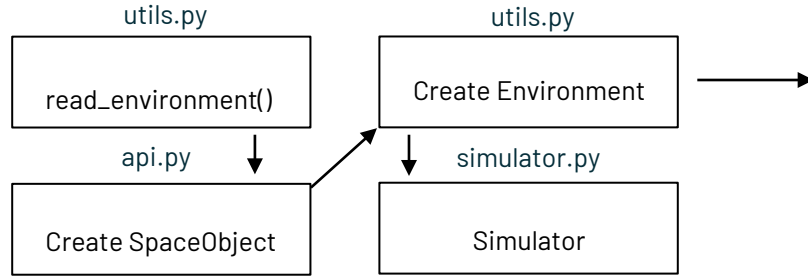
$[(X, Y, Z), (X', Y', Z')]$

- *Lambert method ?*
- *Use only TLE as observations ?*

Pipeline

Agent

Simulator



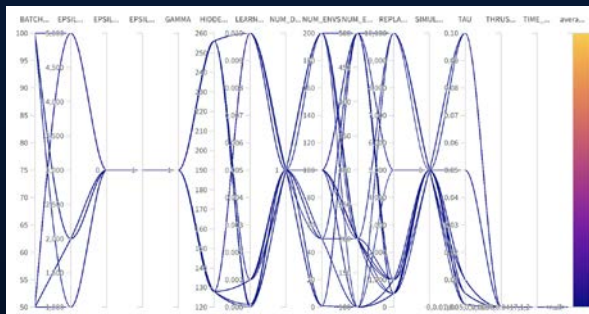
```
class TableAgent(BaseAgent):  
    def __init__(self, action_table=np.array []):  
        """  
        Args:  
            action_table (np.array with shape=(n_actions, 4) or (4) or (0 )):  
                table of actions with columns ["dVx", "dVy", "dVz", "time to request"].  
        """  
        self.action_table = adjust_action_table(action_table)  
        self.action_idx = 0  
  
    def get_action(self, state):  
        """ Provides action for protected object.  
        Args:  
            state (dict): environment state  
            {'coord' (dict):  
                {'st' (np.array with shape (1, 6 )): satellite r and Vx, Vy, Vz coordinates.  
                 'debr' (np.array with shape n_items, 6 ): debris r and Vx, Vy, Vz coordinates.)  
            'trajectory_deviation_coef' (float).  
            'epoch' (pk.epoch): at which time environment state is calculated.  
            'fuel' (float): current remaining fuel in protected SpaceObject. }  
        Returns:  
            action (np.array [dVx, dVy, dVz, time_to_req ]):  
                vector of deltas for protected object (m/s),  
                step in time when to request the next action (mjd2000).  
        """  
        epoch = state["epoch"].mjd2000  
        if self.action_table.size and self.action_idx < self.action_table.shape[0]:  
            action = self.action_table[self.action_idx]  
            self.action_idx += 1  
        else:  
            action = np.array([0, 0, 0, np.nan])  
        return action
```

time_mjd2000	epoch	protected_pos	protected_vel	debris_pos	debris_vel	alert
0	6600.0000 2018-Jan-26 00:00:00	[-4209358.575576871, 6393808.673674893, -1080565.7993943808]	[5942.404053175507, 3627.609290210152, -1726.9822249887982]	[[2713394.019835856, -5280644.467331182, 6687217.586841868], [-496957.2053770637, 5019026.037633914, 5679853.592008259]]	[[[-5985.48861375989, -2476.5442529082225, 1818.0490459728084], [3360.027219101076, 4914.968848441329, -4147.126471761581]]	('is_alert': False, 'info': {})
1	6600.0007 2018-Jan-26 00:01:00.480000	[-3843511.679768749, 6603006.401406782, -1183254.428461531]	[6152.521714303881, 3288.493346969752, -1667.9141353355612]	[[2348766.3802139875, -5425029.346431939, 6790366.05281432], [-293028.64093000744, 5307767.429083958, 5419724.026258173]]	[[[-6069.989596000446, -2297.889672149641, 1593.132833811351], [3381.777273102908, 4630.625922316658, -4452.743071270137]]	('is_alert': False, 'info': {})
2	6600.0014 2018-Jan-26 00:02:00.960000	[-3465541.322440386, 6791376.538647311, -1282210.7711207657]	[6343.208206753268, 2939.046604699317, -1603.592518872451]	[[1979444.158502754, -5558577.62091522, 6879950.104785391], [-88124.02781972336, 5578825.388436893, 5141538.5614142455]]	[[[-6140.796644937557, -2118.2627835560493, 1389.5630667021776], [3392.288463640473, 4330.354465700382, -4744.037122299136]]	('is_alert': False, 'info': {})
3	6600.0021 2018-Jan-26 00:03:01.440000	[-3076640.9493011767, 6958327.315087309, -1377123.1453917958]	[6513.870295530154, 2580.3665031965206, -1534.2201291482263]	[[1606243.829369231, -5681243.215600596, 6956063.977468491], [117074.48328442452, 5831265.328088557, 4846194.911804498]]	[[[-6198.299937592521, -1938.0794949060469, 1147.756761300748], [3391.4870592992083, 4015.1158741124027, -5019.9748159507635]]	('is_alert': False, 'info': {})

Agent(
protected_pos,
protected_vel,
debris_pos,
debris_vel)

Experiments

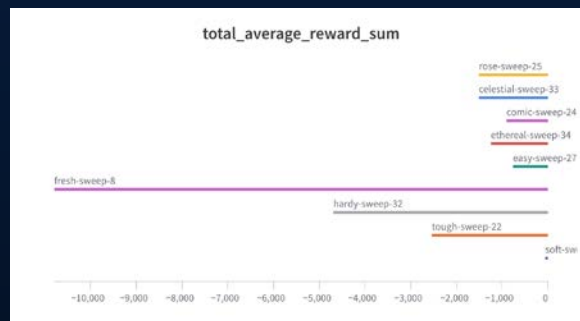
Evaluating best hyper parameters



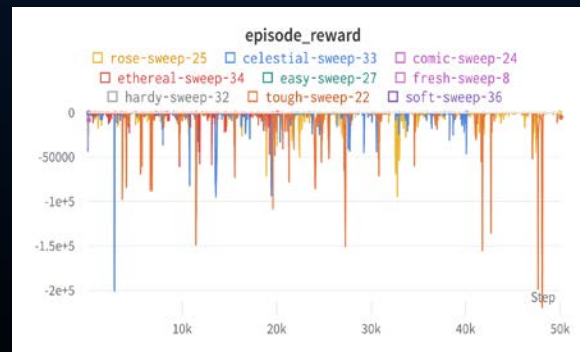
Best loss



Best total reward sums

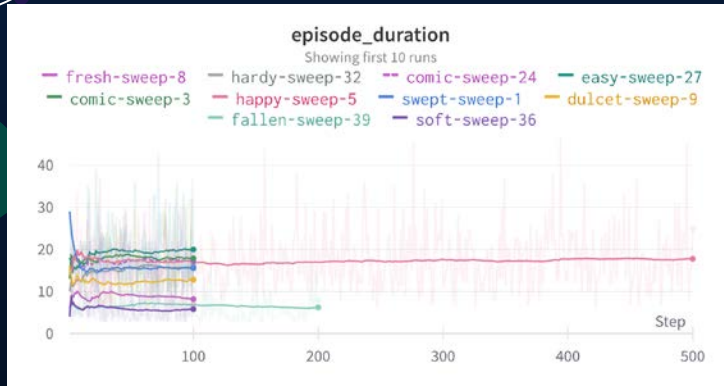


Best episode rewards

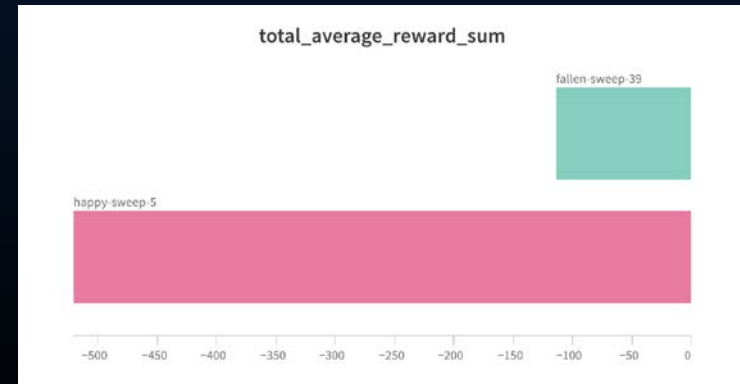
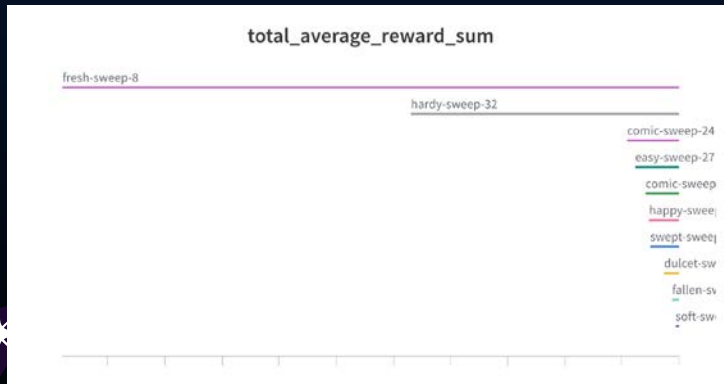


1 environment

All the runs

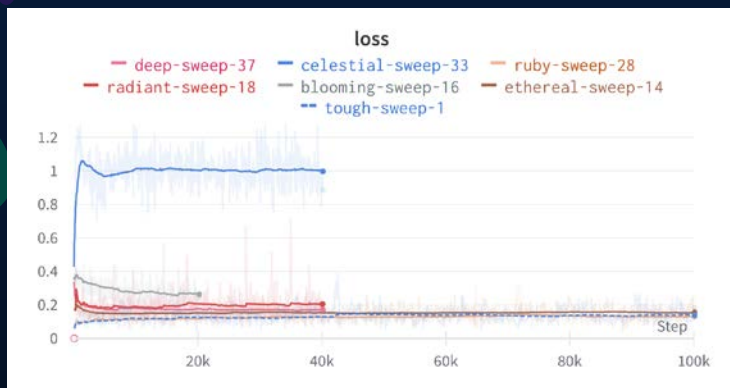


Converging vs diverging

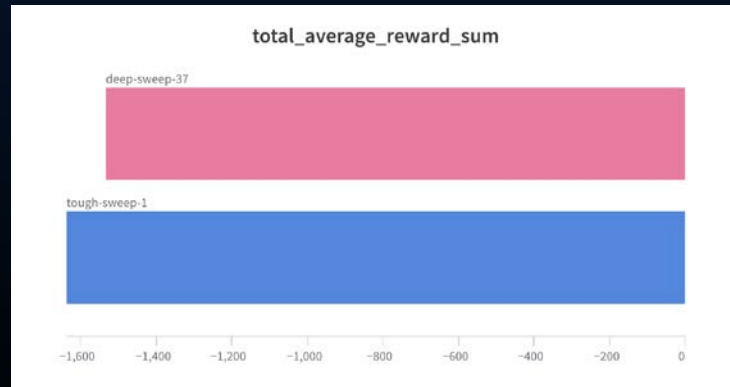
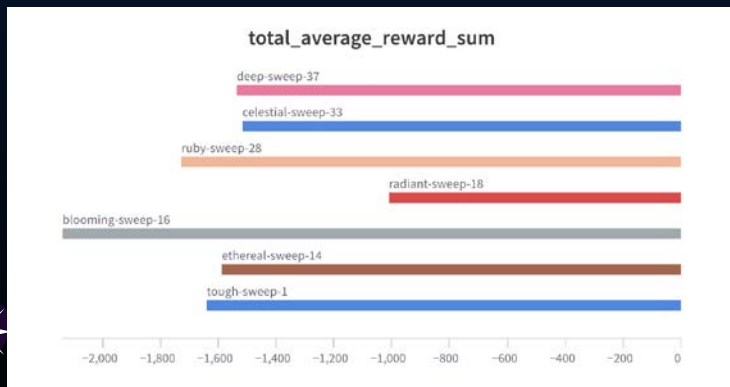


200 environments

All the runs



Converging vs diverging





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Thank You

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